

Instructions: I have mixed up the problems from sections 6.2 and 6.3. When solving each problem:

- (a) Draw a picture which shows a sample “slice”,
- (b) Indicate what method you will be using (i.e. disk, washer, or cylindrical shells),
- (c) set up the integral and solve the problem.

1. Find the volume of the solid obtained by rotating the region bounded by $y = \frac{1}{x}$, $y = 0$, $x = 1$, and $x = 10$ about the x -axis.
2. Find the volume of the solid obtained by rotating the region bounded by $y = 4x - x^2$ and $y = 8x - 2x^2$ about the line $x = -2$.
3. Find the volume of the solid obtained by rotating the region bounded by $y = x$ and $y = \sqrt{x}$ about the line $x = 2$.
4. Find the volume of the solid obtained by rotating the region bounded by $y = x^2 - 4x + 5$ and $y = -x^2 + 4x - 1$ about the line $x = -1$.
5. Find the volume of the solid obtained by rotating the region bounded by $y = x^4$ and $y = \sqrt{\sin(\pi x/2)}$ about the x -axis. (Hint: If you have problems finding the upper limit of integration, your graphing calculator can find the intersection of two curves. Or ask me.)

From 6.5:

1. Find the average value of $f(x) = \cos x$ over the interval $[\pi, 2\pi]$.
2. Find the average value of $g(r) = 3/(1+r)^2$ over the interval $[1, 6]$.