

Let  $c \in \mathbb{R}$ .

11 a)  $f(x) = 3 \cos x - 4 \sec^2 x$

$F(x) = 3 \sin x - 4 \tan x + c$

b)  $f(x) = \frac{x^{27} - 14x^{-1.4} + x^8}{x^3}$   
 $= x^{24} - 14x^{-4.4} + x^5$

$F(x) = \frac{1}{25} x^{25} + \frac{14}{3.4} x^{-3.4} + \frac{1}{6} x^6 + c$

c)  $f(\theta) = 6\theta^2 - 7 \sin \theta$

$F(\theta) = 2\theta^3 + 7 \cos \theta + c$

d)  $f(x) = 6x^{1/2} - x^{1/6}$

$F(x) = \frac{2(6)}{3} x^{3/2} - \frac{6}{7} x^{7/6} + c$

$F(x) = 4x^{3/2} - \frac{6}{7} x^{7/6} + c$

12 a)  $f'(x) = \sin x - x^{1/2}$

redo  $f'(x) = -\cos x - \frac{2}{3} x^{3/2} + c$

$f(x) = -\sin x - \frac{2}{3} (\frac{2}{5}) x^{5/2} + cx + a$ ,  
 $c, a \in \mathbb{R}$

b)  $f'(x) = 8x^3 + 12x + 3, f(1) = 6$

$f(x) = \frac{8}{4} x^4 + 6x^2 + 3x + c$

$f(1) = 2(1)^4 + 6(1)^2 + 3(1) + c = 6$

$c = 6 - 6 - 2 - 3 = -5$

$f(x) = 2x^4 + 6x^2 + 3x - 5$

4

12c  $f'(\theta) = 2 \cos \theta + \sec^2 \theta, f(\frac{\pi}{3}) = 4, -\frac{\pi}{2} < \theta < \frac{\pi}{2}$

$f(\theta) = 2 \sin \theta + \tan \theta + c$

$f(\frac{\pi}{3}) = 2 \sin \frac{\pi}{3} + \tan \frac{\pi}{3} + c = 4$

$2(\frac{\sqrt{3}}{2}) + \sqrt{3} + c = 4$

$c = 4 - 2\sqrt{3}$

$f(\theta) = 2 \sin \theta + \tan \theta + 4 - 2\sqrt{3}$

12d  $f''(x) = 2 + \cos x, f(0) = -1, f(\frac{\pi}{2}) = 0$

$f'(x) = 2x + \sin x + c$

$f(x) = x^2 - \cos x + cx + a$

$f(0) = 0^2 - \cos 0 + c(0) + a = -1$

$-1 + a = -1$

$a = 0$

$f(\frac{\pi}{2}) = 0: (\frac{\pi}{2})^2 - \cos \frac{\pi}{2} + c \frac{\pi}{2} + 0 = 0$

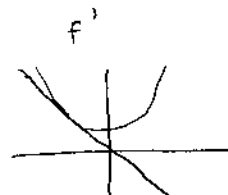
$\frac{\pi^2}{4} - 0 + c \frac{\pi}{2} = 0$

$c = -\frac{\pi^2}{4} \cdot \frac{2}{\pi} = -\frac{\pi}{2}$

$f(x) = x^2 - \cos x - \frac{\pi}{2} x$

13)  $f'(x) = x^3$  &  $x + y = 0 \Rightarrow y = -x$  is tangent to the graph.

$f(x) = \frac{x^4}{4} + c$



$y = -x$   
 $\Rightarrow \frac{y}{0} - a = -(x+a) \quad y+1 = \frac{-(x-1)}{-x+1} \Rightarrow y = -1$   
 $\Rightarrow f'(a) = -1 \Rightarrow a^3 = -1 \Rightarrow a = -1$

So  $f(-1) = \{$

$f(-1) = \frac{1}{4} + c = 1$

$\Rightarrow c = \frac{3}{4}$

$f(x) = \frac{x^4}{4} + \frac{3}{4}$