

$$2a) y = 3x^9 - 7x^6 - 3x + 1$$

$$y' = 27x^8 - 42x^5 - 3$$

$$y' = 27(8)x^7 - 42(5)x^4$$

$$2b) y = \tan(3x)$$

$$y' = 3\sec^2(3x) = 3(\sec 3x)^2$$

$$y'' = 6\sec(3x)(\sec 3x)(\tan 3x) \cdot 3$$

$$= 18\sec^2(3x)\tan(3x)$$

$$3a) 3x^2 - 5y^3 = x$$

$$6x - 15y^2 \frac{dy}{dx} = 1$$

$$\frac{dy}{dx} = \frac{1-6x}{-15y^2}$$

$$b) 5xy + \cos x = \sec y$$

$$5x \frac{dy}{dx} + y \cdot 5 - \sin x = \sec y \tan y \frac{dy}{dx}$$

$$5y - \sin x = (\sec y \tan y - 5x) \frac{dy}{dx}$$

$$\frac{dy}{dx} = \frac{5y - \sin x}{\sec y \tan y - 5x}$$

$$4) \sqrt{x+2} + \sqrt{y} = 3$$

Goal: Tangent line @ (2, 1)

$$\frac{1}{2}(x+2)^{-\frac{1}{2}} + \frac{1}{2}(y)^{-\frac{1}{2}} \frac{dy}{dx} = 0$$

plug in  $x=2, y=1$

$$\frac{1}{2}\left(\frac{1}{2+2}\right)^{-\frac{1}{2}} + \frac{1}{2}\left(\frac{1}{1}\right)^{-\frac{1}{2}} \frac{dy}{dx} = 0$$

$$\frac{1}{2} \cdot \frac{1}{2} + \frac{1}{2} \frac{dy}{dx} = 0$$

$$\frac{1}{2} \frac{dy}{dx} = -\frac{1}{4}$$

$$\frac{dy}{dx} = -\frac{1}{2} @ (2, 1)$$

Ans  $y - 1 = -\frac{1}{2}(x - 2)$

$$5) f(x) = \sin^2 x$$

Goal: tangent line @  $x = \frac{\pi}{3}$

$$f\left(\frac{\pi}{3}\right) = \left[\sin\left(\frac{\pi}{3}\right)\right]^2 = \left(\frac{\sqrt{3}}{2}\right)^2 = \frac{3}{4}$$

$$f'(x) = 2\sin x \cos x$$

$$f'\left(\frac{\pi}{3}\right) = 2\sin\frac{\pi}{3}\cos\frac{\pi}{3} = 2 \cdot \frac{\sqrt{3}}{2} \cdot \frac{1}{2} = \frac{\sqrt{3}}{2}$$

$$y - \frac{3}{4} = \frac{\sqrt{3}}{2}\left(x - \frac{\pi}{3}\right)$$

$$6) g(x) = \cos \pi x + 3$$

Goal: Tangent line @  $x = -2$

$$g(-2) = \cos(-2\pi) + 3$$

$$= 1 + 3 = 4$$

$$g'(x) = -\pi \sin(\pi x)$$

$$g'(-2) = -\pi \sin(-2\pi) = 0$$

$$y - 4 = 0(x + 2) \Rightarrow y = 4$$

7) Where is tangent line to  $f(x) = -x^2 - 6$  parallel to  $y = 4x - 1$ .

Where is  $f'(x) = 4$ ?

$$f'(x) = -2x$$

$$\text{Solve } -2x = 4 \Rightarrow x = -2 \text{ pt } (-2, -10)$$

8) Where is tangent line of  $g(x) = x^3 - 3x$  perp. to  $5y - 3x - 8 = 0$

$$g'(x) = 3x^2 - 3$$

$$\text{Next, } 5y - 3x - 8 = 0 \Rightarrow y = \frac{3}{5}x + \frac{8}{5}$$

want perp. so need  $g'(x) = -\frac{5}{3}$ .

$$\text{Solve } 3x^2 - 3 = -\frac{5}{3}$$

$$3x^2 = 3 - \frac{5}{3} \Rightarrow x^2 = 1 - \frac{5}{9} = \frac{4}{9} \Rightarrow x = \pm \frac{2}{3}$$

pts  $\left(\frac{2}{3}, \frac{-46}{27}\right), \left(-\frac{2}{3}, \frac{46}{27}\right)$

$$g\left(\frac{2}{3}\right)$$

$$g\left(-\frac{2}{3}\right)$$